

Sol (i) $S = \{2, 4, 5, 7, 9\}$, upper bound ~~is~~ 9
lower bound = 2
 $\Rightarrow S$ is bounded.

(ii) $S = \{1, 2, 3, \dots\}$, lower bound = 1
upper bound ~~is~~ not exist.
 $\Rightarrow S$ is not bounded.

(iii) $S = \{-1, -2, -3, \dots\}$
upper bound = -1
lower bound = not exist
ie; S is bounded above but not bounded below.

(iv) $S = \{1, 2, 3, \dots\}$
lower bound = 1
~~lower~~ upper bound doesn't exist.
 $\Rightarrow S$ is bounded below but not bounded above.

Q2 find the infimum and supremum of the following sets, which of these belongs to the set?

(i) $[1, 3, 5, 7, 9]$ smallest member = 1

Sol let $S = \{1, 3, 5, 7, 9\}$, $\inf S = 1$ $\sup S = 9$
greatest member = 9 $\inf$ & $\sup$ both exist $\Rightarrow S$ is bdd

(ii) $\{-1, -\frac{1}{2}, -\frac{1}{3}, -\frac{1}{4}, \dots\}$

Sol let $S = \{-1, -\frac{1}{2}, -\frac{1}{3}, -\frac{1}{4}, \dots\} = \{-\frac{1}{n} : n \in \mathbb{N}\}$
 $\inf S = -1$ $\sup S = 0$ but $0 \notin S$, $-1 \in S$
 $\Rightarrow S$ is bdd, smallest member of $S = -1$